

# The Hubble tension: approaches, solutions and challenges

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# The expansion of the Universe

## The Hubble rate $H$

Current expansion rate of the Universe  
 $H_0$

Us and our experiments

Primordial plasma

Cosmic microwave background

Radiation domination

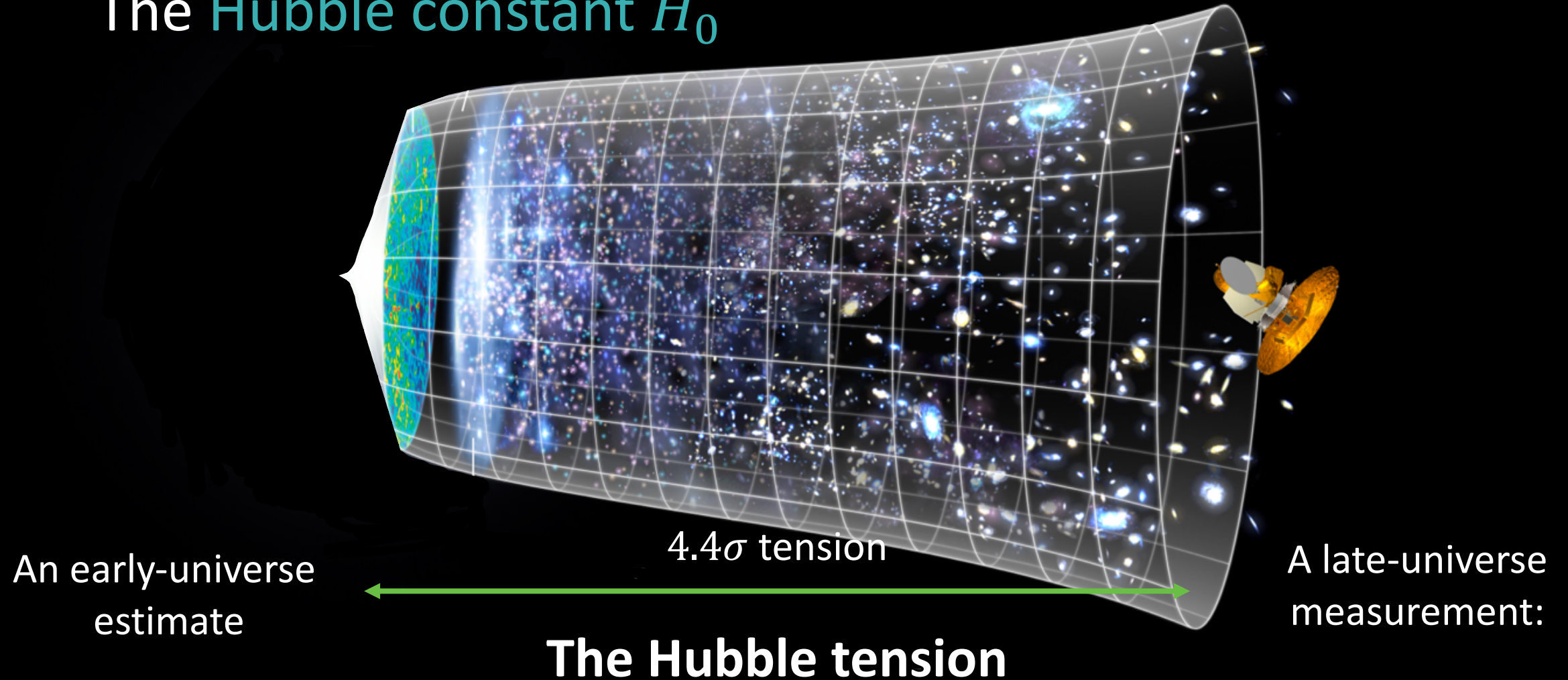
Matter domination

Dark energy domination



# The expansion of the Universe today

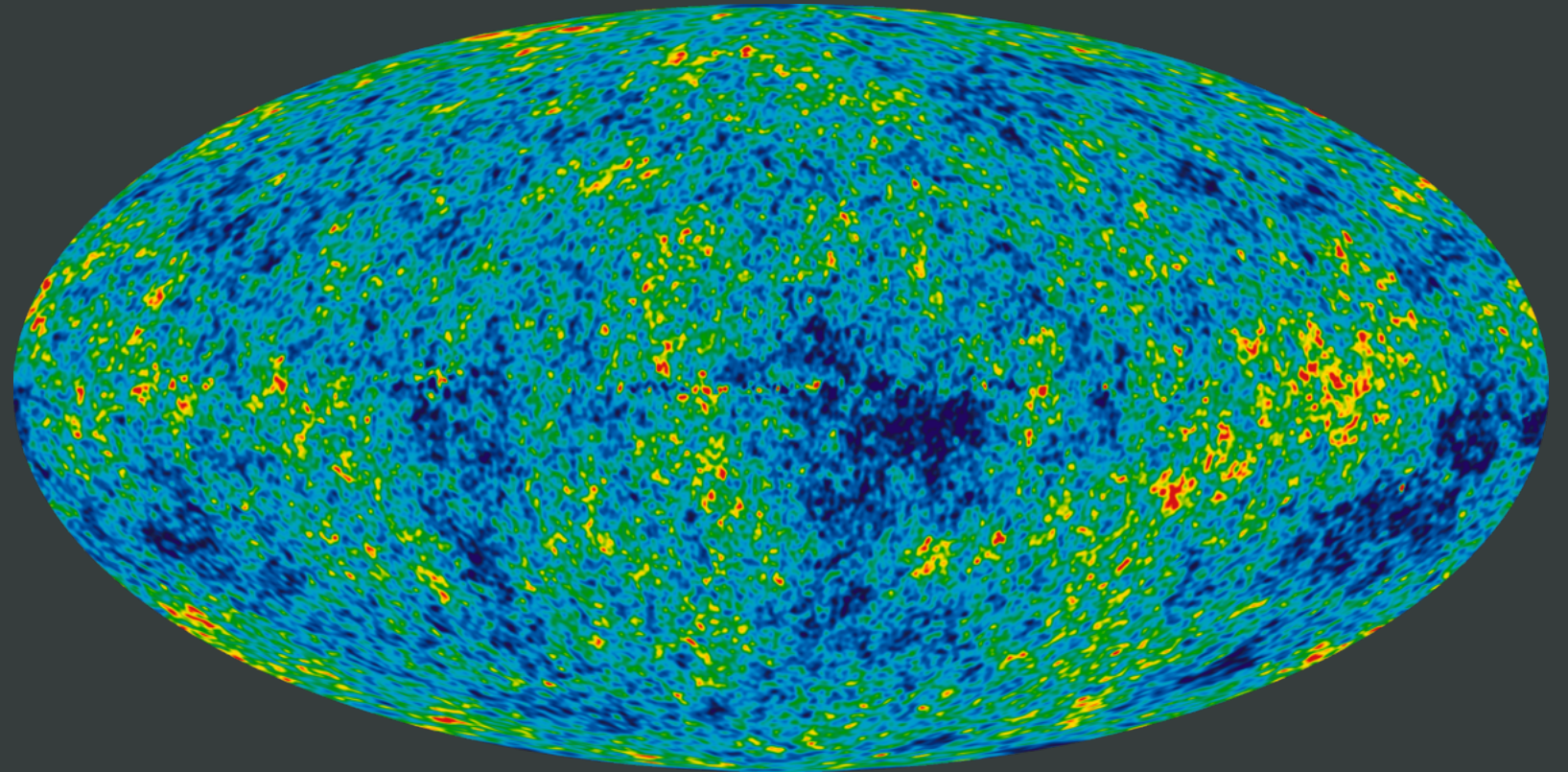
## The Hubble constant $H_0$



# Cosmic microwave background

## The oldest light in the Universe

Density imprint  
produced by sound  
waves in the early  
universe



Source: WMAP

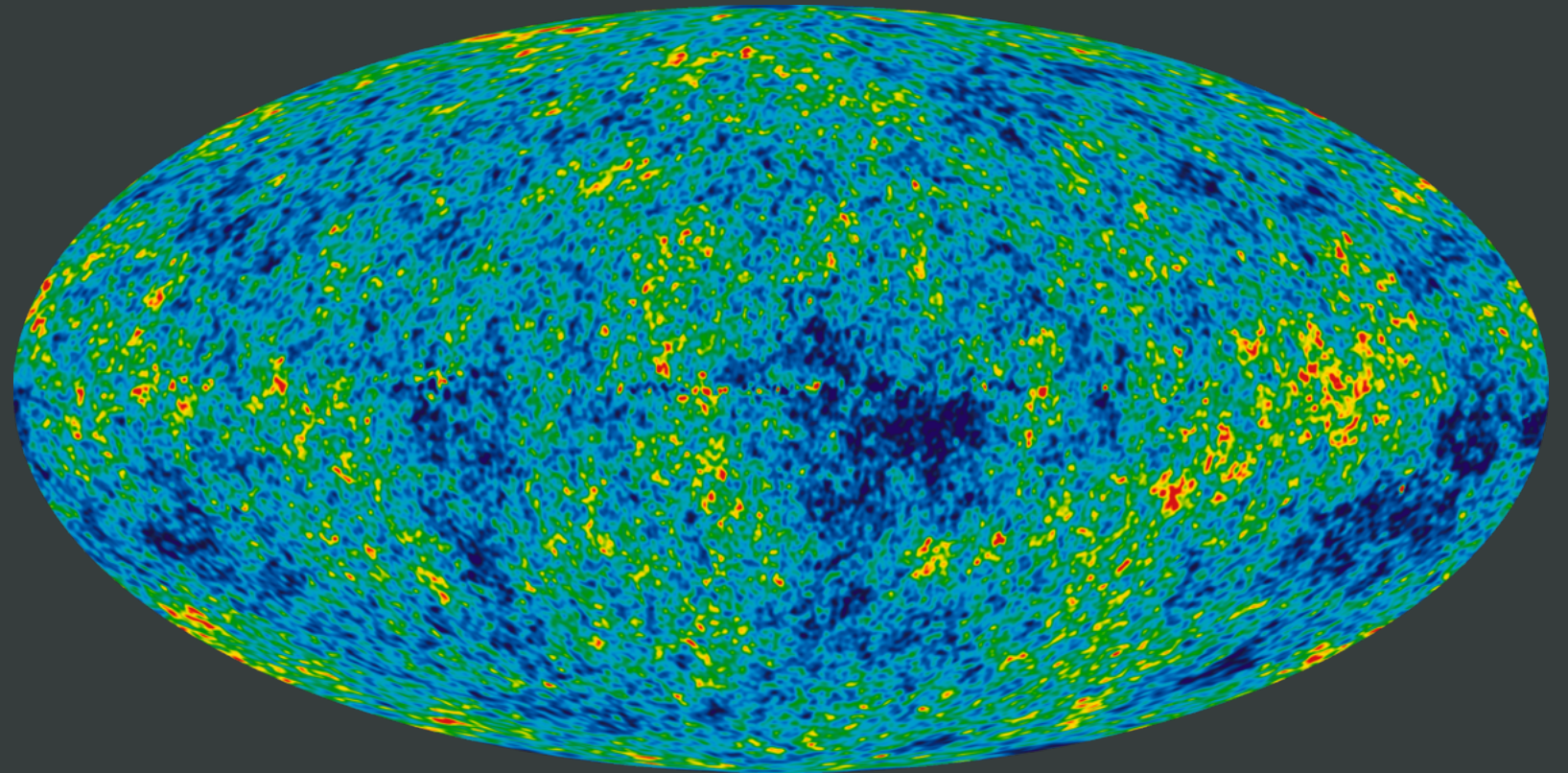
# Cosmic microwave background

## The oldest light in the Universe

Density imprint  
produced by sound  
waves in the early  
universe

Maximum  
variation at  
 $\theta_* \sim 1^\circ$  scales

Farthest distance  
that sound waves  
travelled  $\sim r_s$   
The sound horizon



Source: WMAP

# The standard model of cosmology

## $\Lambda$ CDM

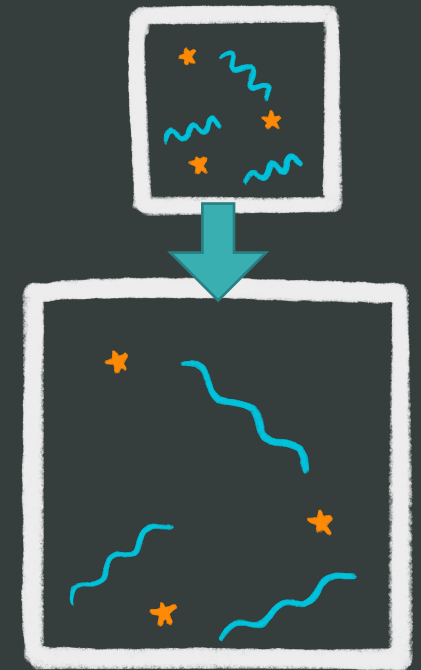
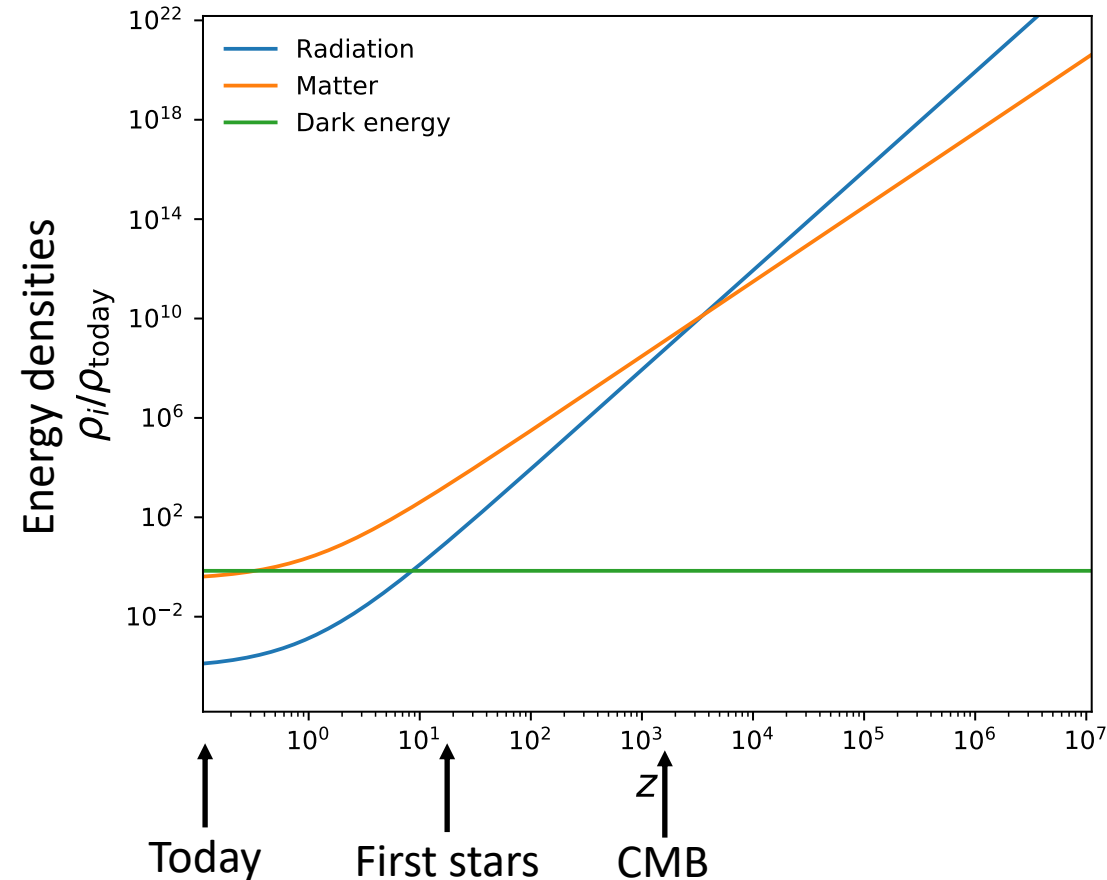
Matter density  $\propto z^3$   
Cold dark matter  
CDM

Radiation density  $\propto z^4$

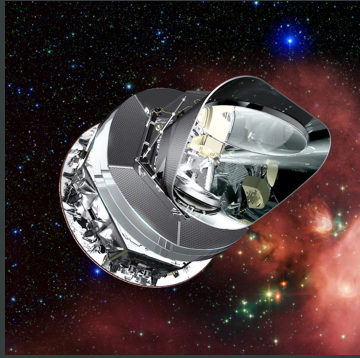
Dark energy density  $\propto z^0$   
Cosmological  
constant  $\Lambda$

$$H(z) \propto \sqrt{\rho_{tot}(z)}$$

Expansion rate  $\propto$  Energy content

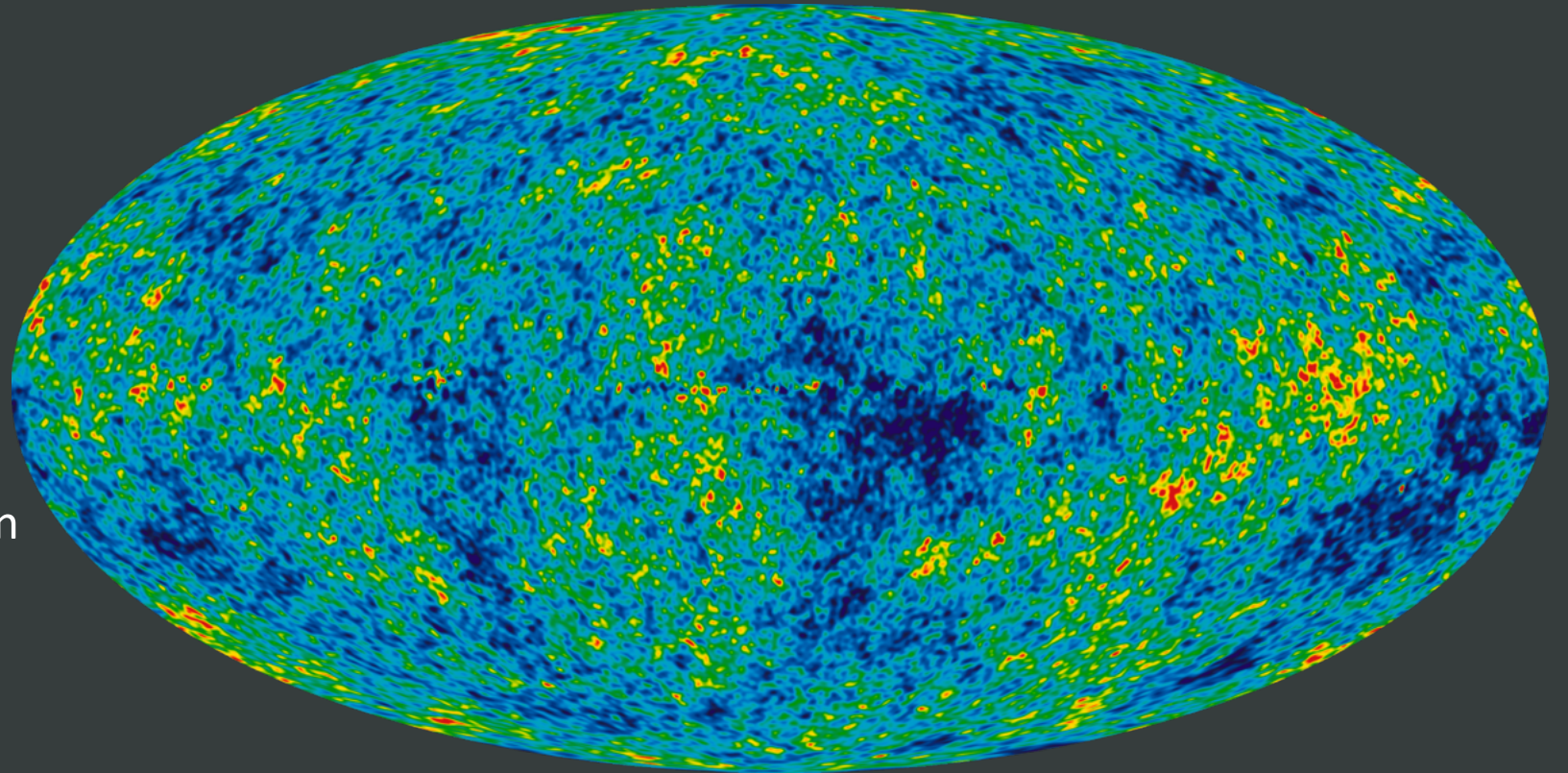


# Cosmic microwave background and the $\Lambda$ CDM model



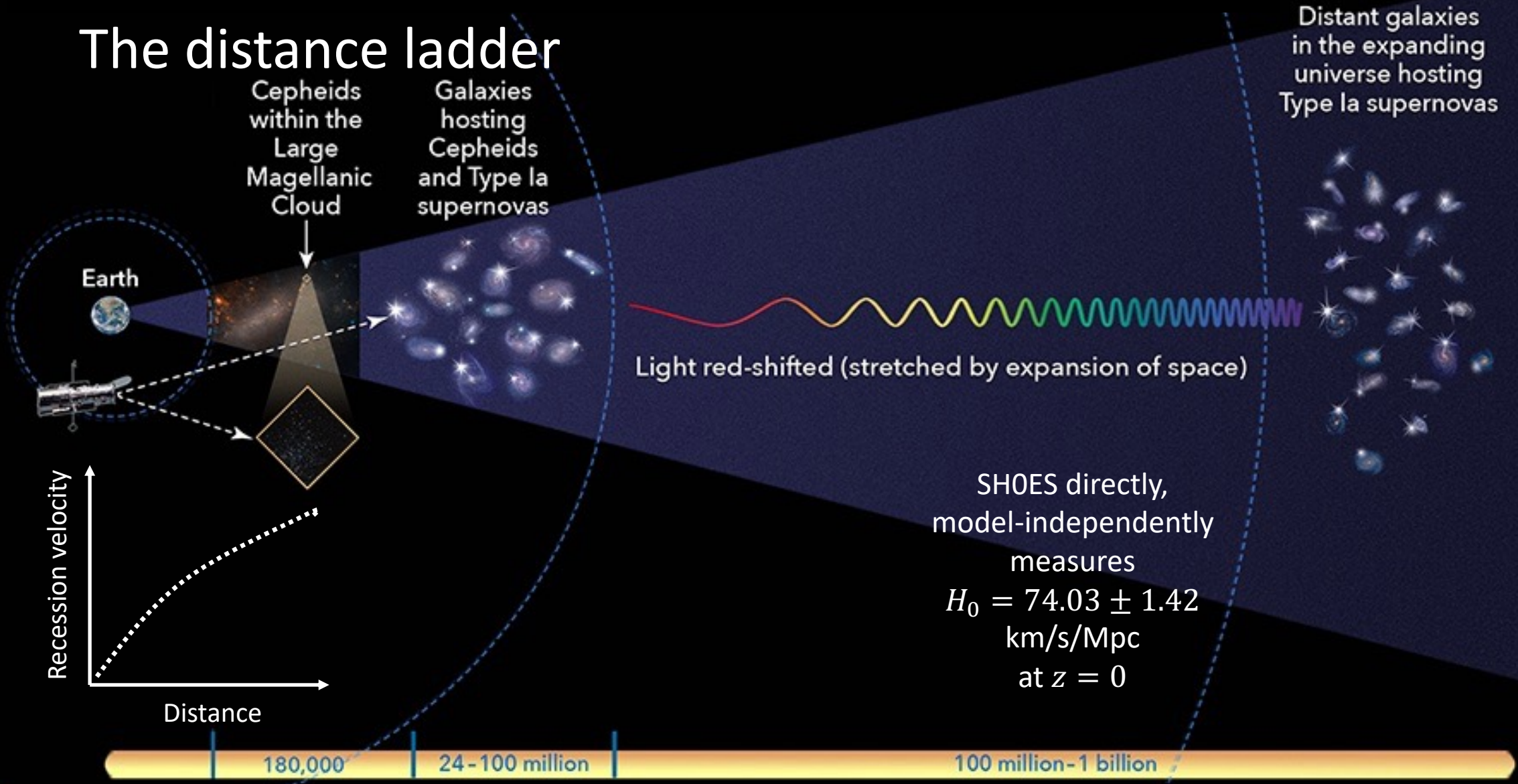
Planck fits  $\Lambda$ CDM to constrain  
 $H_0 = 67.4 \pm 0.5$  km/s/Mpc  
by observing the Universe  
at early times

Planck [1807.06209]



Source: WMAP

# The distance ladder





Fit  $\Lambda$ CDM to the early universe  
 $H_0 = 67.4 \pm 0.5$  km/s/Mpc

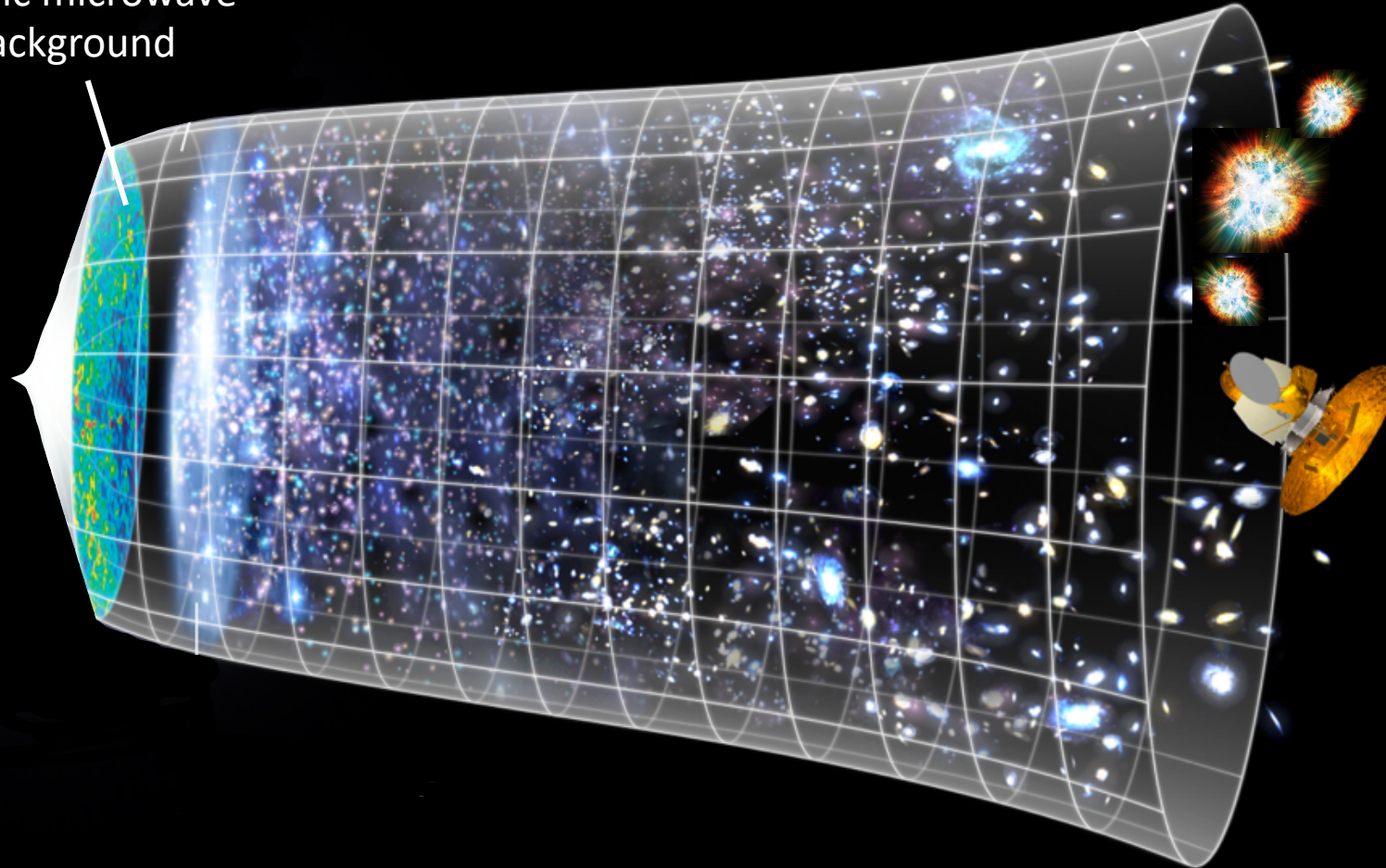
4.4 $\sigma$  tension

Directly measure in current universe  
 $H_0 = 74.03 \pm 1.42$  km/s/Mpc

# The Hubble tension

Cosmic microwave background

Early universe + cosmological assumptions



Late universe + astrophysical assumptions

CMB estimation < Direct measurement

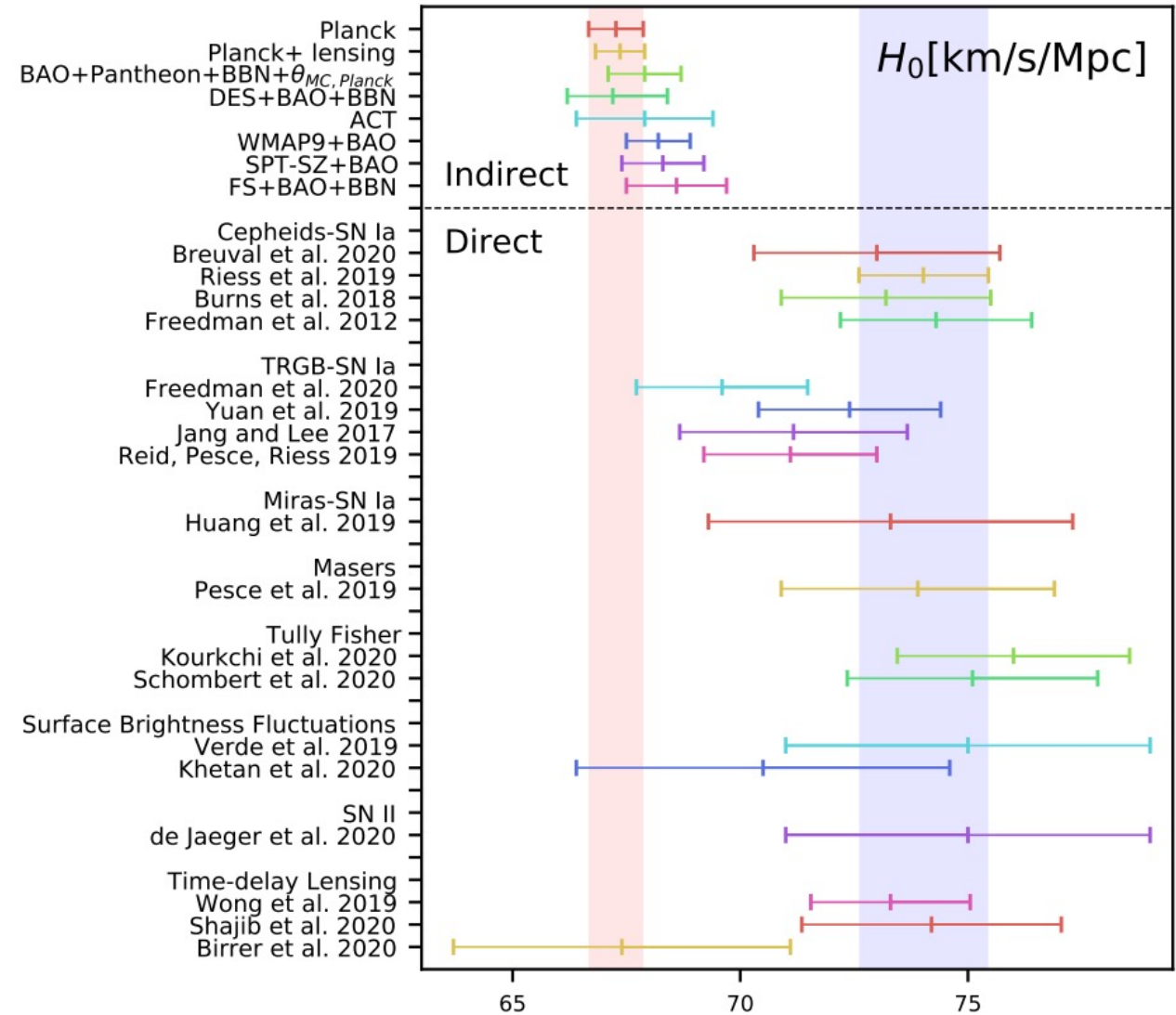
# The Hubble tension Current state – headache



Discrepancy between the early and late universe?

Is  $\Lambda$ CDM wrong?

Di Valentino [2011.00246]



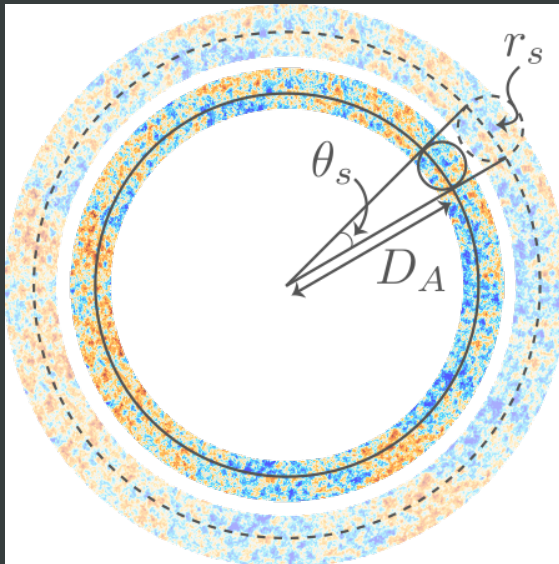
# This talk

→ Approaches to theoretically resolving the Hubble tension

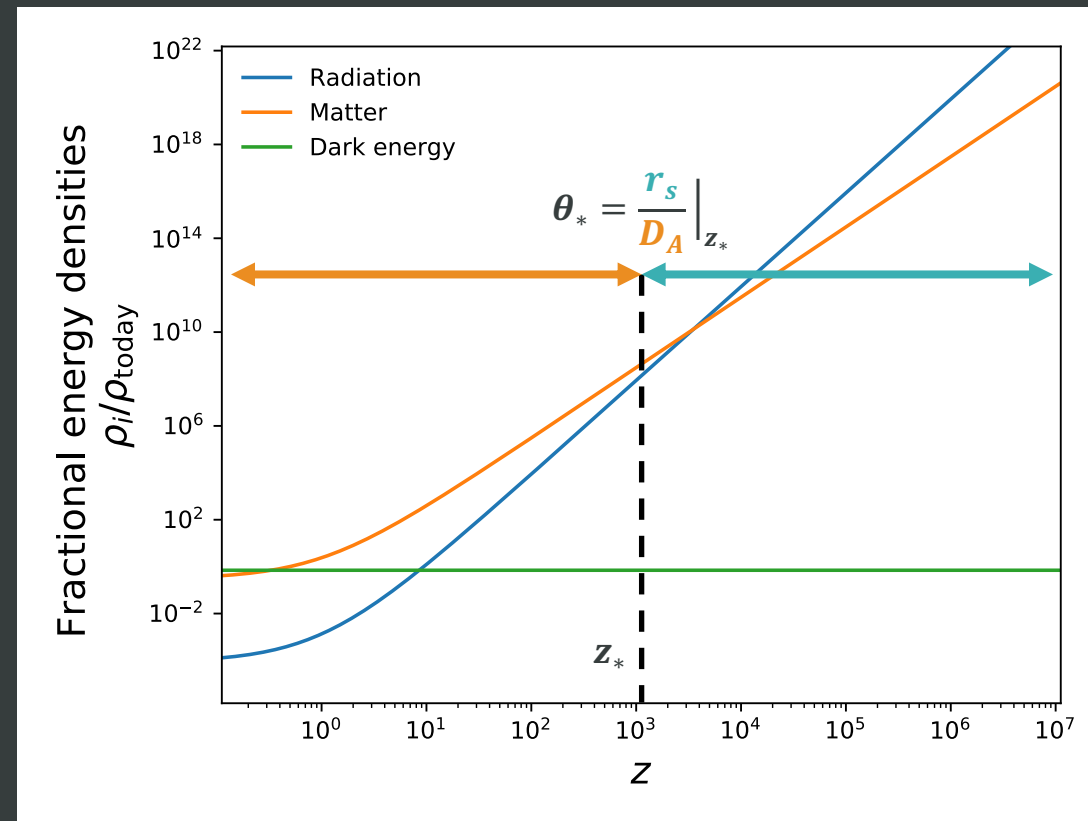
- Solutions to  $H_0$ : early dark energy (EDE) models
- Challenges: the large-scale structure tension

# When to add new physics? Early universe

Precisely measured  $\theta_*$  is an approximate proxy for CMB peak locations



Cartoon by Tristan L. Smith



$$D_A \propto 1/H_{post}$$

$$\theta_* \sim \frac{r_s}{1/H_{post}} \sim r_s H_0$$

For constant  $\theta_*$  ,  
 $r_s \propto 1/H_0$

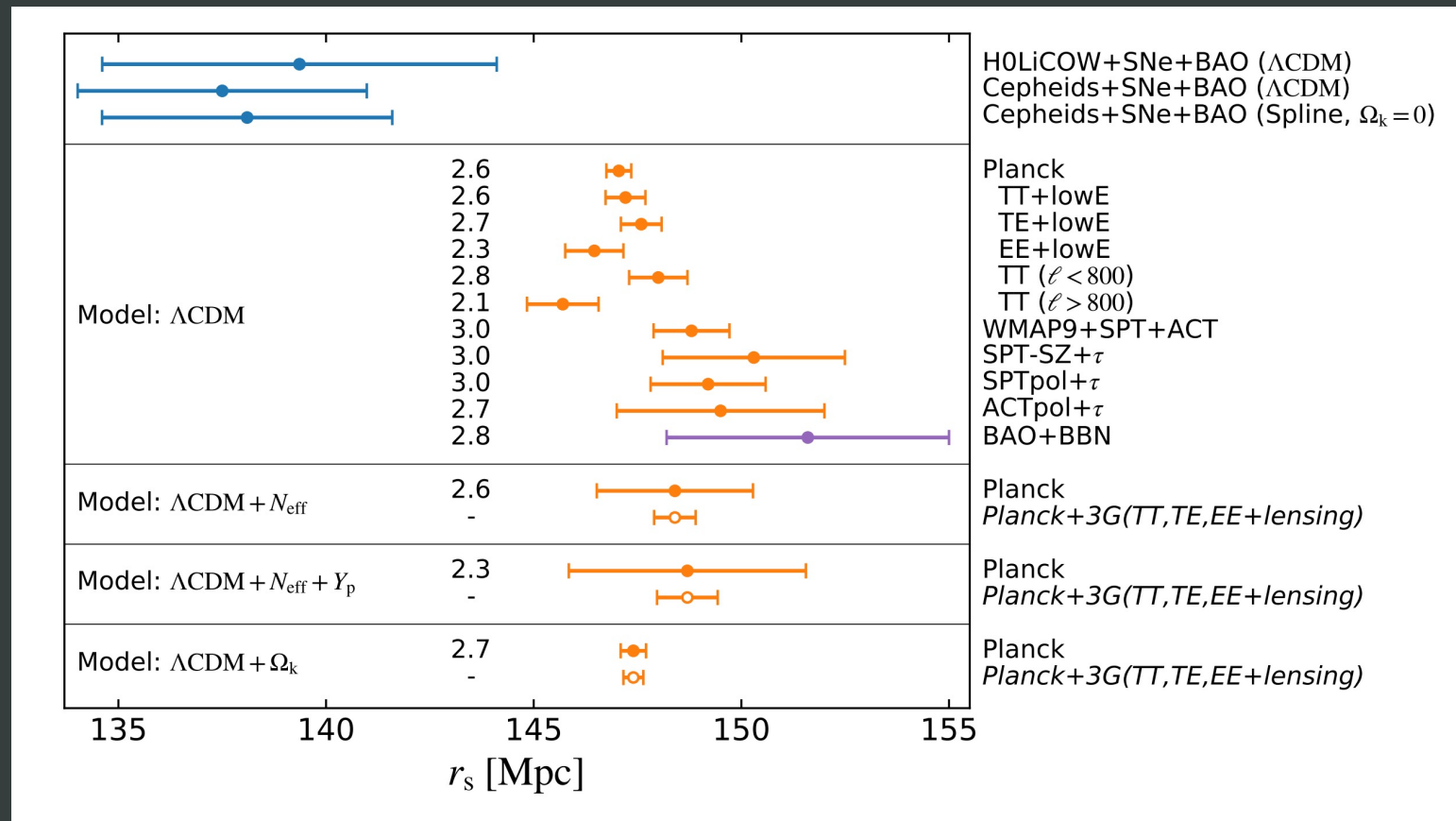
In support of an early universe modification:  
Planck [1807.06209]  
Bernal et al [1607.05617]  
Evslin et al [1711.01051]  
Aylor et al [1811.00537]

# Hubble tension $\leftrightarrow$ Sound horizon tension

Distance ladder  
+ BAO  $\rightarrow r_s$

CMB  $r_s + \text{BAO}$   
 $\rightarrow H_0$

No CMB data



Higher  $H_0$  measured

Lower  $H_0$  inferred

Lower  $H_0$  inferred

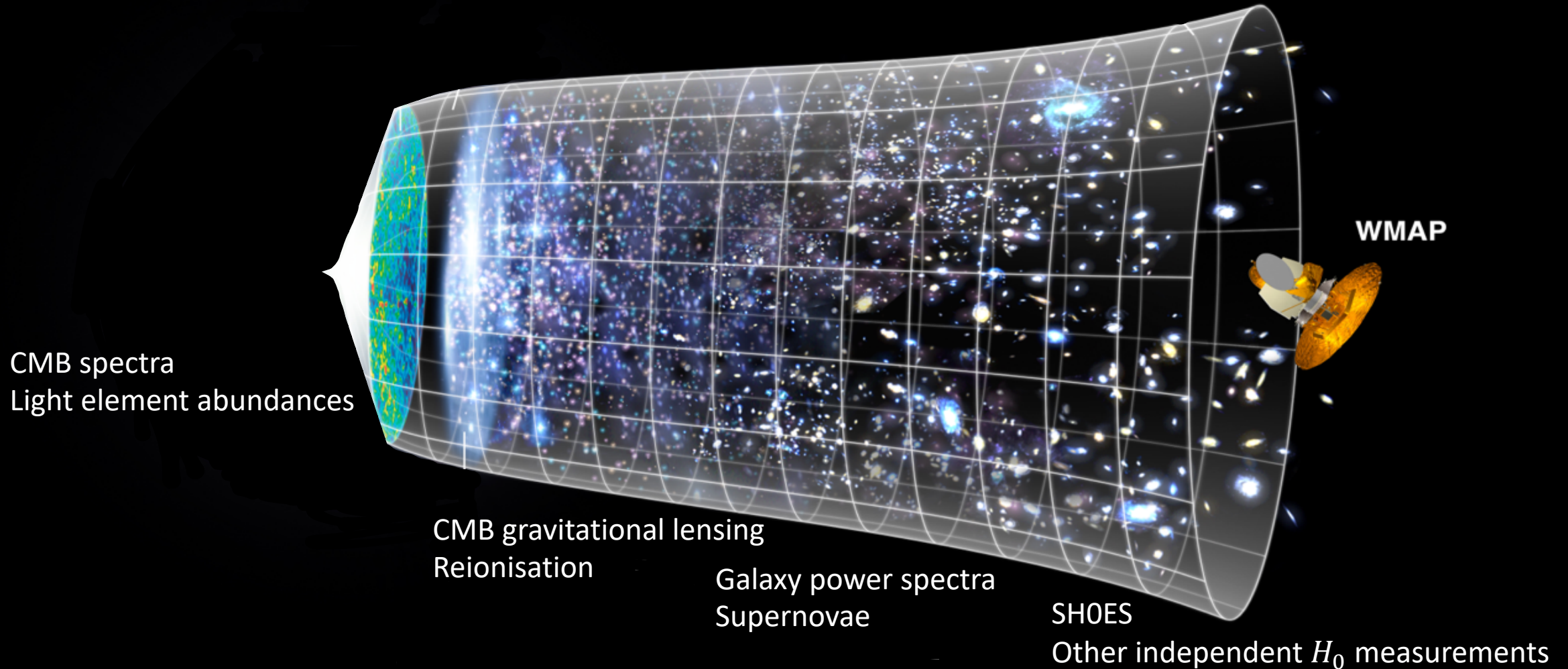
Aylor et al [1811.00537]

# Approaches to a solution

Requirements:

- Keep  $\theta_*$  fixed (or keep CMB peaks fixed) such that  $r_s \propto 1/H_0$
- Decrease  $r_s \propto 1/H_{pre}(z)$ , so increase the pre-CMB expansion rate

# How to add new physics? Leave late universe unchanged



# Approaches to a solution

Requirements:

- Keep  $\theta_*$  fixed (or keep CMB peaks fixed) such that  $r_S \propto 1/H_0$
- Decrease  $r_S \propto 1/H_{pre}(z)$ , so increase the pre-CMB expansion rate
- Leave  $D_A \propto 1/H_{post}(z)$  unchanged, so modification must disappear at late times



# This talk

✓ Approaches to theoretically resolving the Hubble tension

→ Solutions to  $H_0$ : early dark energy (EDE) models

- Challenges: the large-scale structure tension



# Hubble solutions

## Reduce $r_s$

Farthest distance that  
sound waves travelled

$$\sim r_s \sim \theta_*$$

Electrons and protons  
have to combine  
sooner

The Universe must expand faster than  $\Lambda$ CDM at very early times, before the CMB was emitted

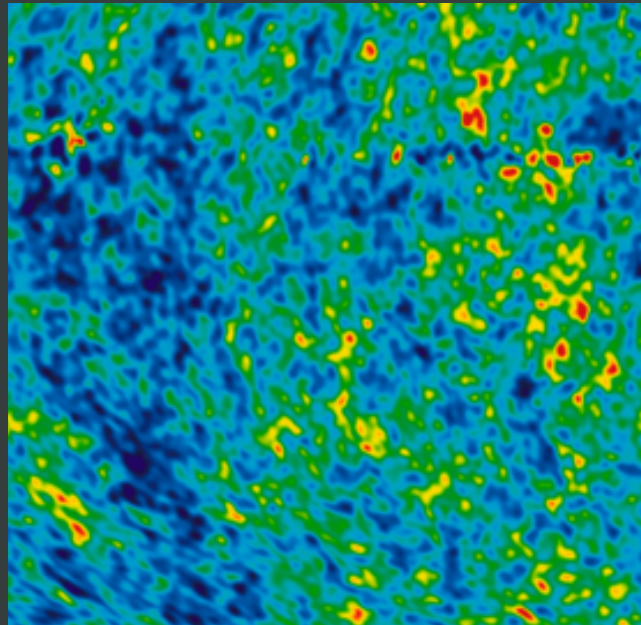
Sound waves travel a  
shorter distance if CMB is  
emitted earlier

The Universe  
has to cool through  
expansion faster

WMAP, NASA

# Hubble solutions

## Effect of early dark energy



Observed CMB

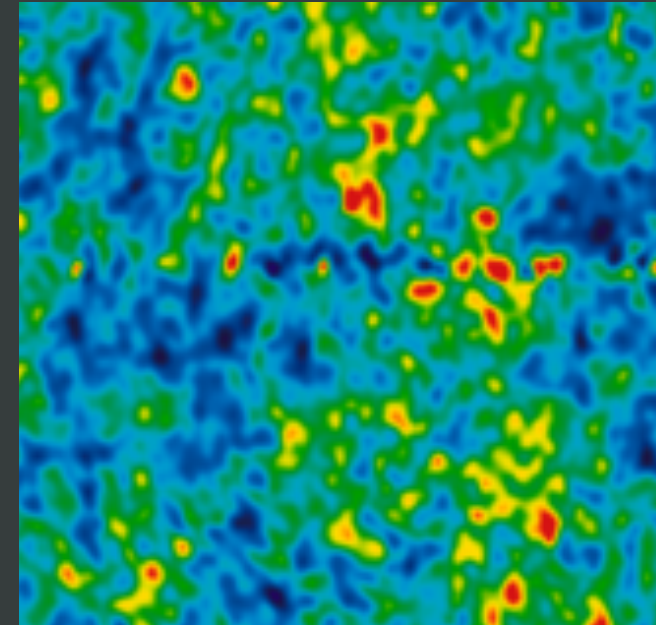


Increase  
 $H_0$



Decrease  
 $r_s$

Add  
early dark energy



Disagreement with  
observed CMB

# Approaches to a solution

Requirements:

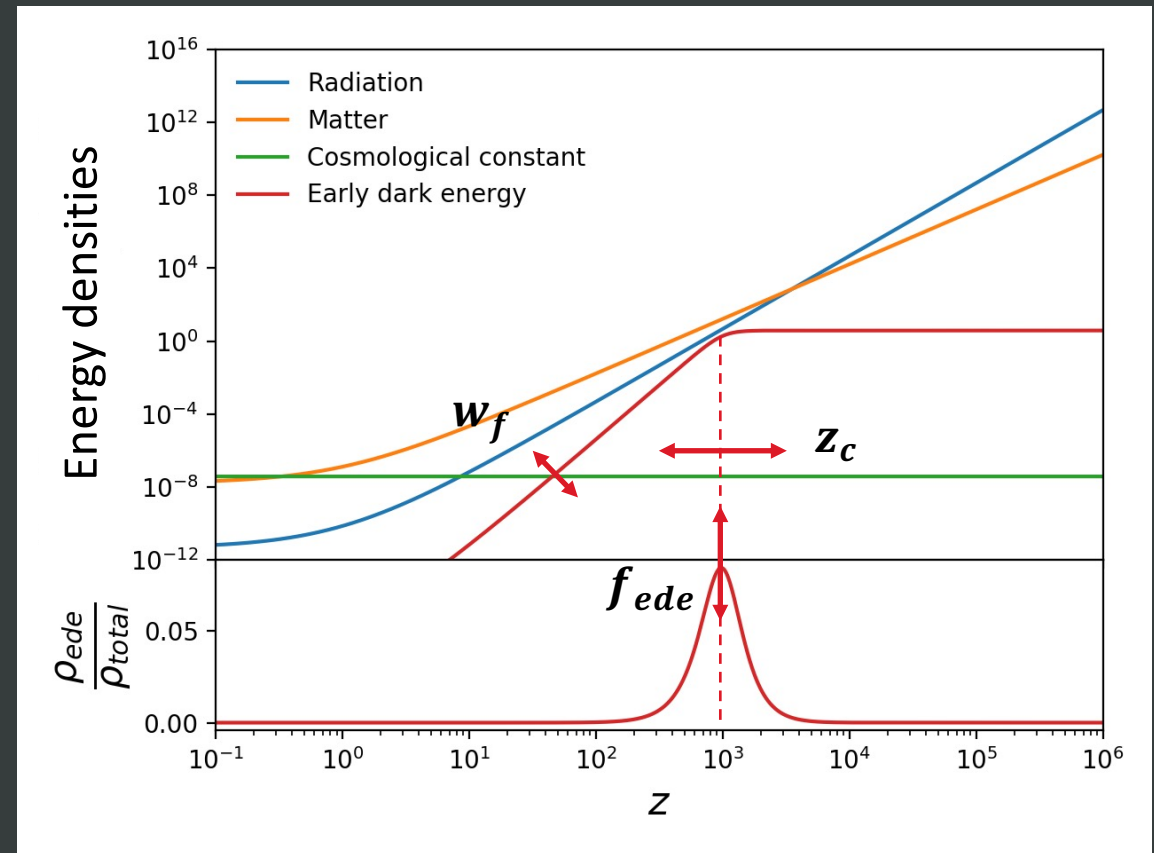
- ✓ Keep  $\theta_*$  fixed (or keep CMB peaks fixed) such that  $r_S \propto 1/H_0$
- ✓ Decrease  $r_S \propto 1/H_{pre}(z)$ , so increase the pre-CMB expansion rate
- Leave  $D_A \propto 1/H_{post}(z)$  unchanged, so modification must disappear at late times

# Early dark energy (EDE)

Additional energy component with the properties:

- $\Lambda$ -like behaviour initially
- Then dilutes faster than matter as  $w_f$
- Localised peak in  $f_{ede} = \frac{\rho_{ede}}{\rho_{total}}$  at  $z_c$

$f_{ede}$  - how much EDE  
 $z_c$  - when EDE appears  
 $w_f$  (or  $n$ ) - how fast is disappears



# Approaches to a solution

Requirements:

- ✓ Keep  $\theta_*$  fixed (or keep CMB peaks fixed) such that  $r_S \propto 1/H_0$
- ✓ Decrease  $r_S \propto 1/H_{pre}(z)$ , so increase the pre-CMB expansion rate
- ✓ Leave  $D_A \propto 1/H_{post}(z)$  unchanged, so modification must disappear at late times

# Early dark energy Models

- Dark energy at early times, the Hubble parameter, and the string axiverse  
TK & Kamionkowski [1608.01309]
- Cosmological implications of ultralight axionlike fields  
Poulin, TK et al [1806.10608]
- Early Dark Energy Can Resolve The Hubble Tension  
Poulin, TK et al [1811.04083]
- Thermal Friction as a Solution to the Hubble Tension  
Berghaus & TK [1911.06281]
- Dark energy from the string axiverse. Kamionkowski, Pradler & Walker [1409.0549]
- Rock 'n' Roll Solutions to the Hubble Tension. Agrawal et al [1904.01016]
- Axion-Dilaton Destabilization and the Hubble Tension. Alexander & McDonough [1904.08912]
- Acoustic Dark Energy: Potential Conversion of the Hubble Tension. Lin et al [1905.12618]
- Oscillating scalar fields and the Hubble tension: a resolution with novel signatures. Smith, Poulin, Amin [1908.06995]
- New Early Dark Energy. Neidermann & Sloth [1910.10739]
- Early Dark Energy from Massive Neutrinos as a Natural Resolution of the Hubble Tension. Sakstein & Trodden [1911.11760]
- Unifying Inflation with Early and Late-time Dark Energy in F(R) Gravity. Nojiri et al [1912.13128]
- Is the Hubble tension a hint of AdS phase around recombination? Ye & Piao [2001.02451]
- Unified framework for early dark energy from  $\alpha$ -attractors. Braglia et al [2005.14053]
- A novel early Dark Energy model. Garcia, Castaneda, Tejeiro [2009.07357]
- Neutrino-Assisted Early Dark Energy: Theory and Cosmology. Gonzalez et al [2011.09895]

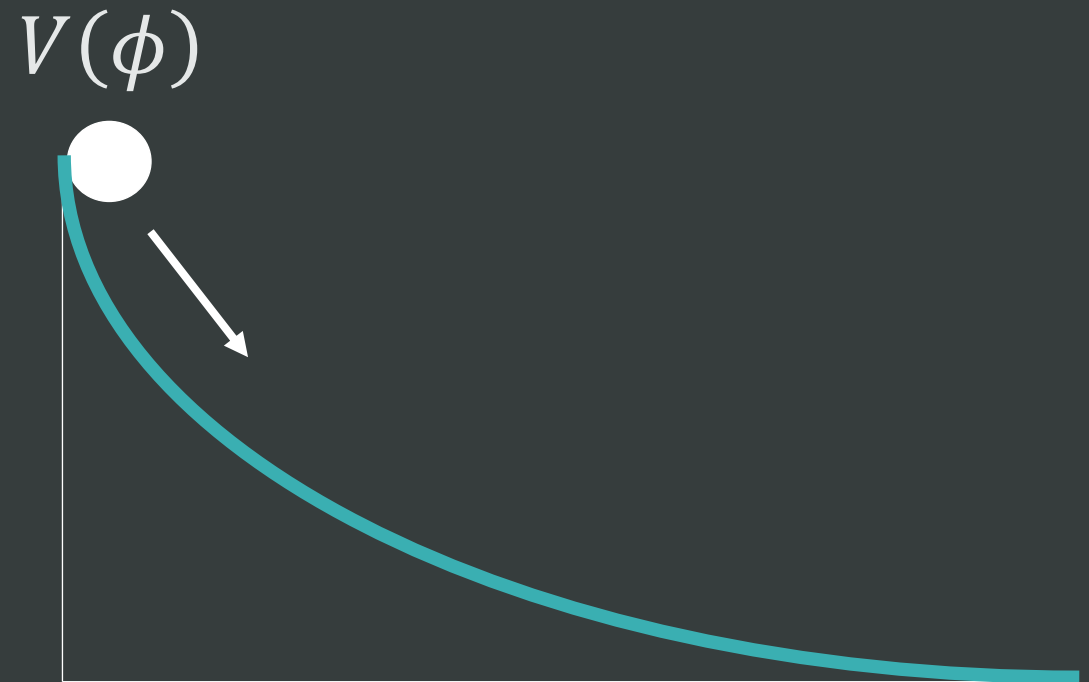
# Early dark energy Models

Dissipative axion (DA)

Uncoupled scalar experiences **Hubble friction**. Uncoupled DR dilutes as  $(1+z)^4$

$$\ddot{\phi} + (3H) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr}$$



Berghaus & Karwal [1911.06281]



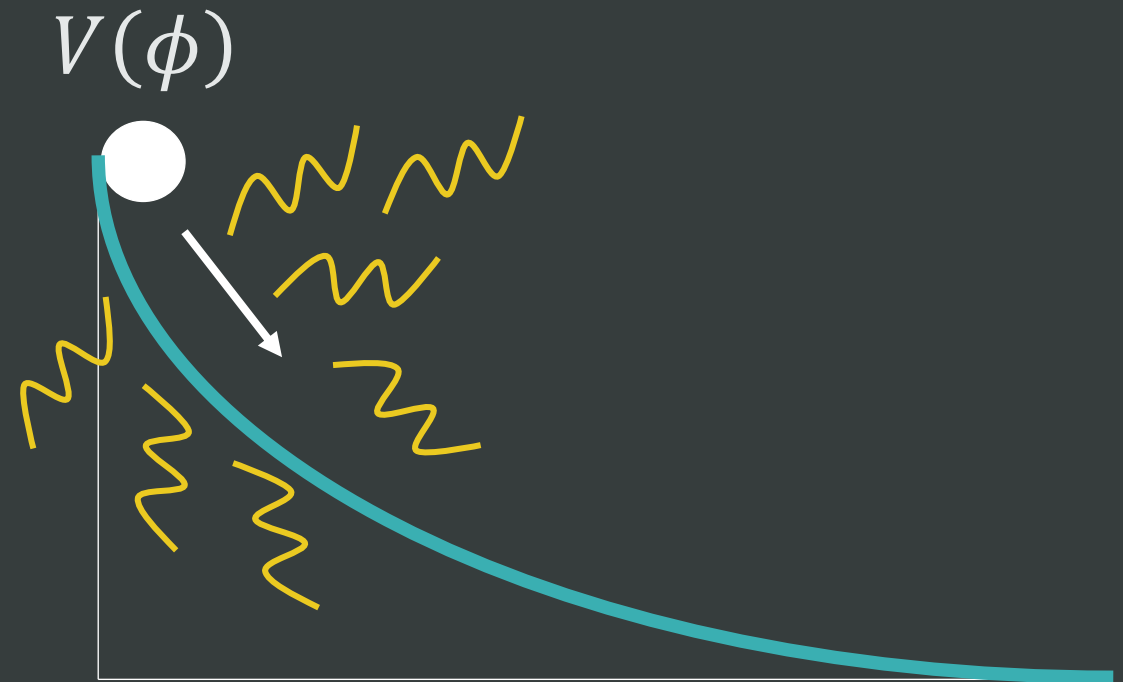
# Early dark energy Models

Dissipative axion (DA)

Scalar coupled to DR **additionally** experiences **thermal friction**

$$\ddot{\phi} + (3H + \Upsilon(T_{dr})) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$



Berghaus & Karwal [1911.06281]

# Early dark energy Models

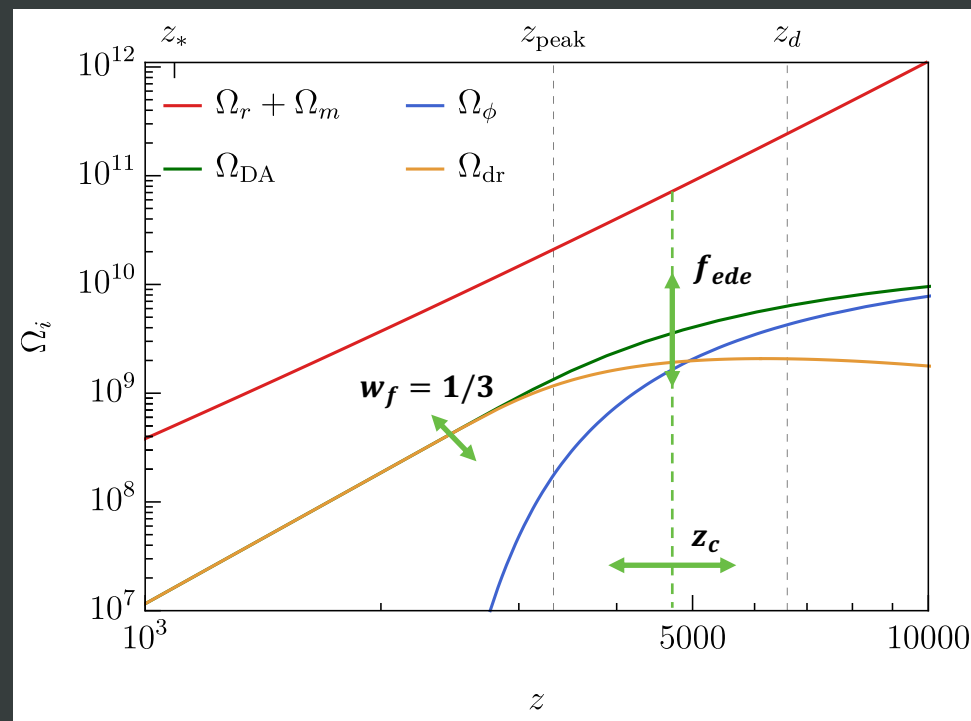
Dissipative axion (DA)

$$\ddot{\phi} + (3H + \Upsilon(T_{dr})) \dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$

$$\begin{aligned} m, \phi_i &\rightarrow f_{ede} \\ m, \Upsilon(T_{dr}) &\rightarrow z_c \\ w_f &= 1/3 \end{aligned}$$

Robust to choice of  $V(\phi)$



Berghaus & Karwal [1911.06281]

# Early dark energy Models

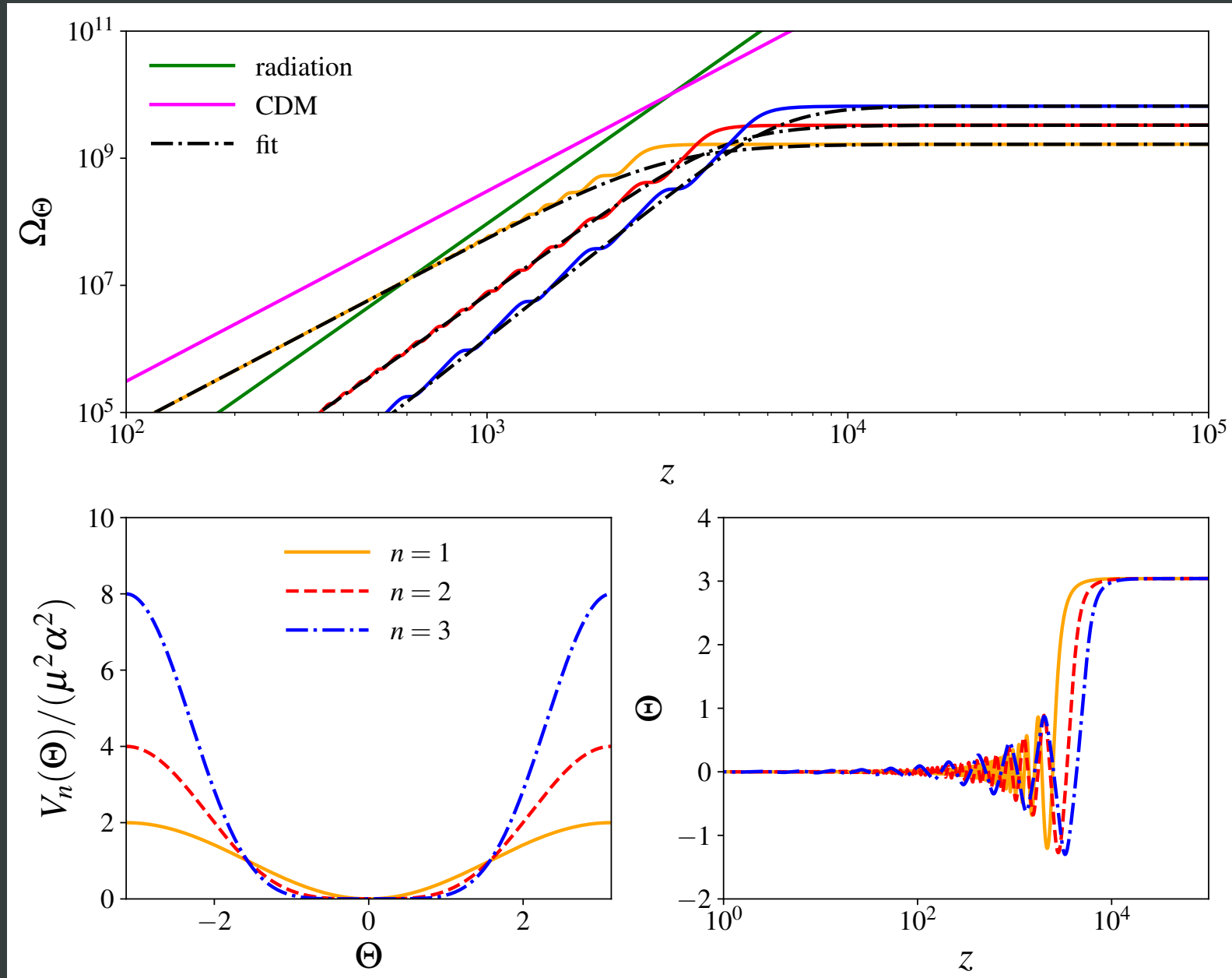
Ultra-light axion-like (ULA) particles

$$V(\phi) \propto (1 - \cos(\phi))^n$$

$$w_f = \frac{n-1}{n+1}$$

$$\phi_i, f, m \leftrightarrow f_{ede}, z_c$$

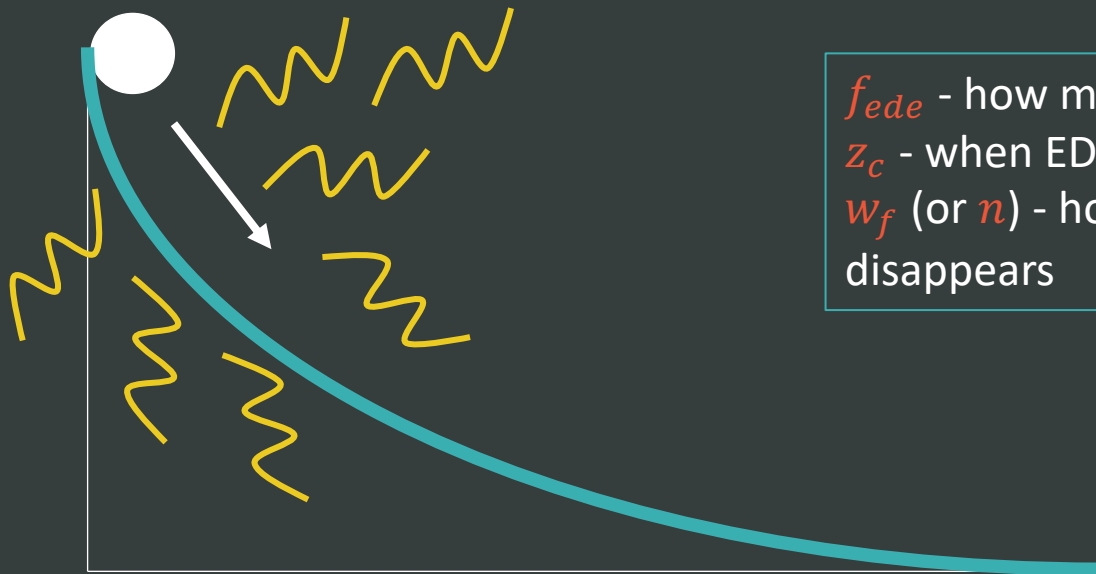
Poulin, TK, et al [arxiv:1806.10608]



# Early dark energy Models

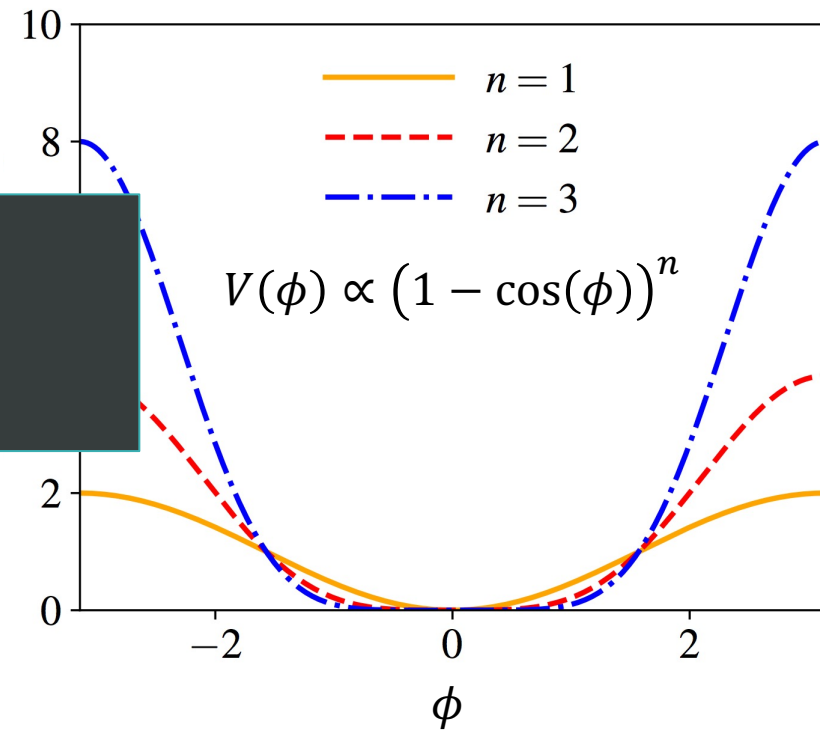
## Dissipative Axion

$$V(\phi) \sim \phi^2$$



$f_{ede}$  - how much EDE  
 $z_c$  - when EDE appears  
 $w_f$  (or  $n$ ) - how fast it disappears

## Ultra-light axion inspired (ULA) potential



Berghaus & Karwal [1911.06281]

Poulin, TK, et al [arxiv:1806.10608]

# Early dark energy Solutions

Based on

- CMB temperature, polarisation and lensing data from Planck 2015
- Local Hubble measurement from SHOES 2018
- Baryon acoustic oscillations
- Pantheon supernovae

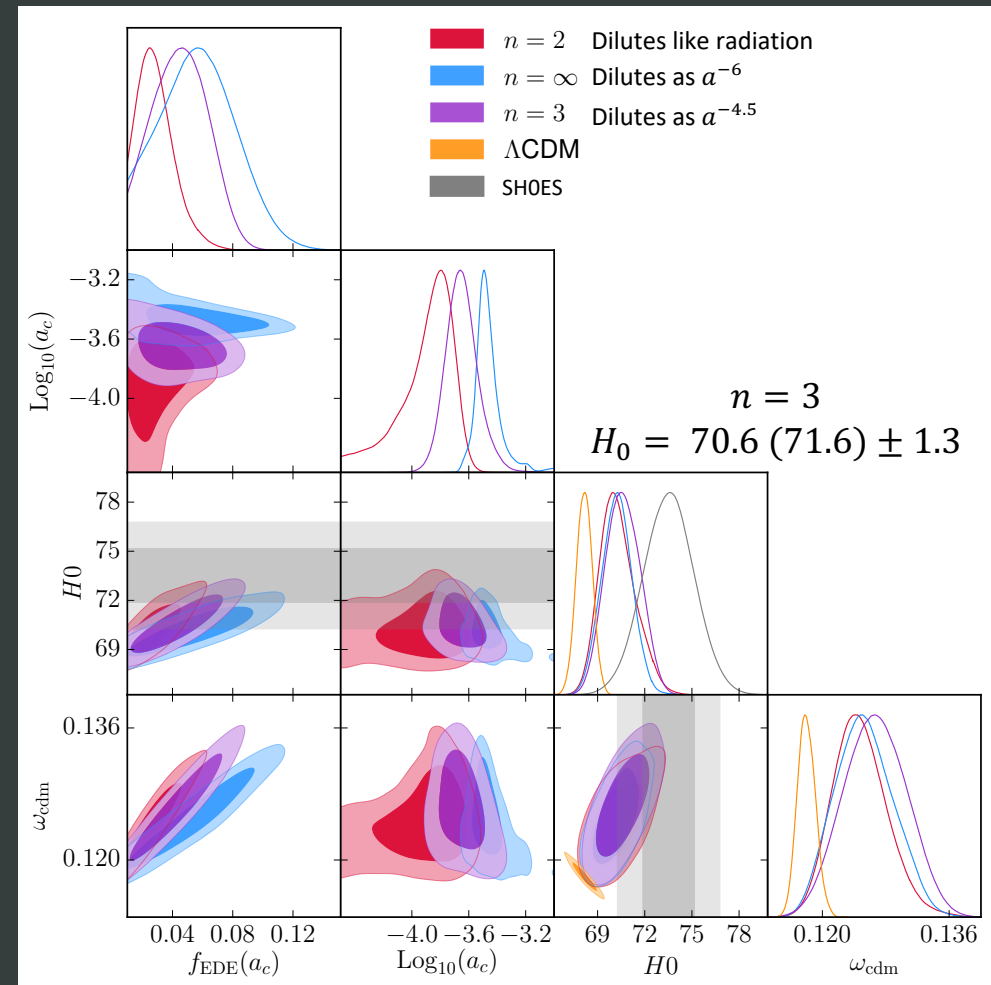
$\omega_{cdm}$  = fractional amount of cold dark matter today

$f_{ede}(a_c)$  = fractional energy density in the axion field at critical redshift  $z_c \approx 1/a_c$

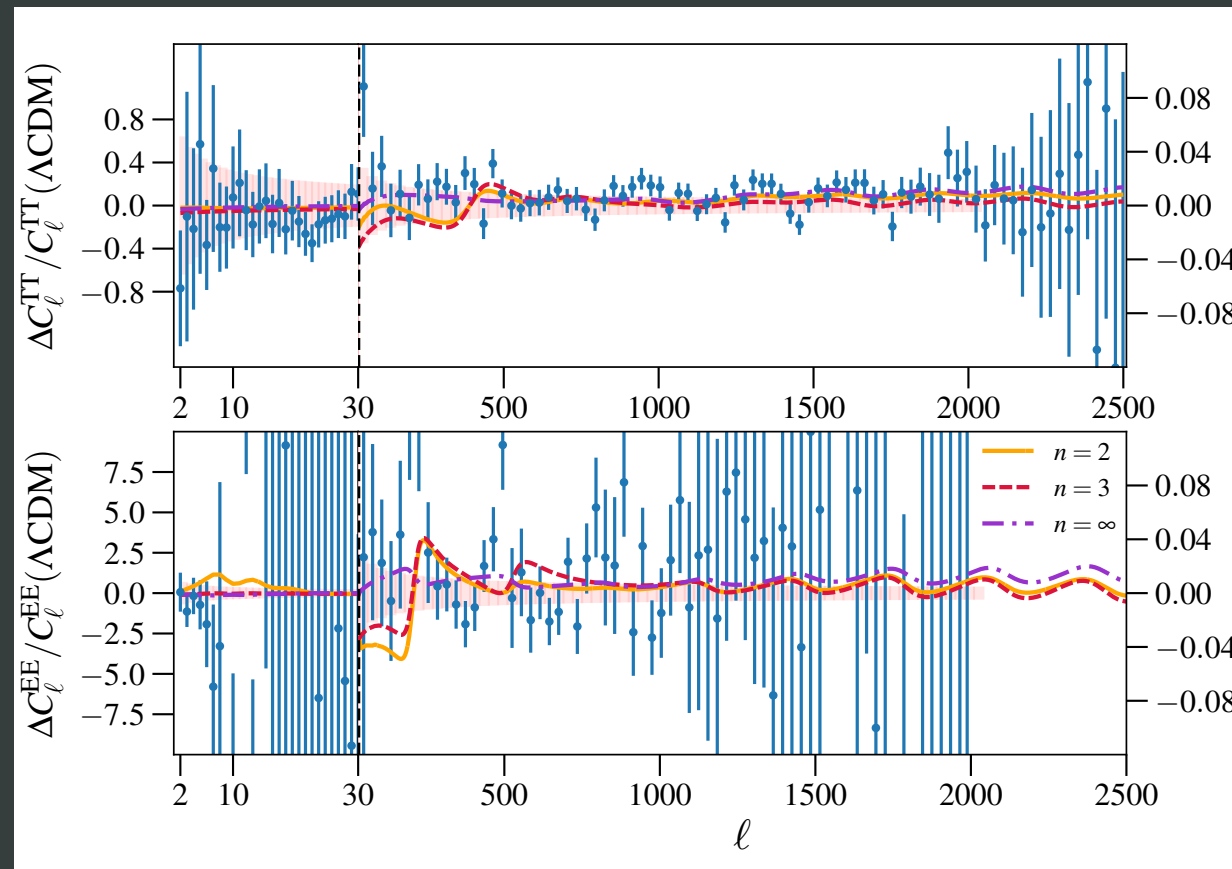
As before,  $w_f = \frac{n-1}{n+1}$

Poulin, TK et al [1811.04083]

## Phenomenological EDE (ULA fluid)



# Early dark energy Detection



Could detect EDE in  
cosmic-variance-limited,  
high- $\ell$   
CMB polarisation data

Poulin, TK et al [1811.04083]

# Early dark energy New concordance model?

Cosmologists



Is this the new concordance model?

# This talk

- ✓ Approaches to theoretically resolving the Hubble tension
- ✓ Solutions to  $H_0$ : early dark energy (EDE) models

→ Challenges: the large-scale structure tension



Fit  $\Lambda$ CDM to the early universe  
 $H_0 = 66.93 \pm 0.62$   
km/s/Mpc

4.4 $\sigma$  tension

# The Hubble tension

Directly measure in current universe  
 $H_0 = 74.03 \pm 1.42$   
km/s/Mpc

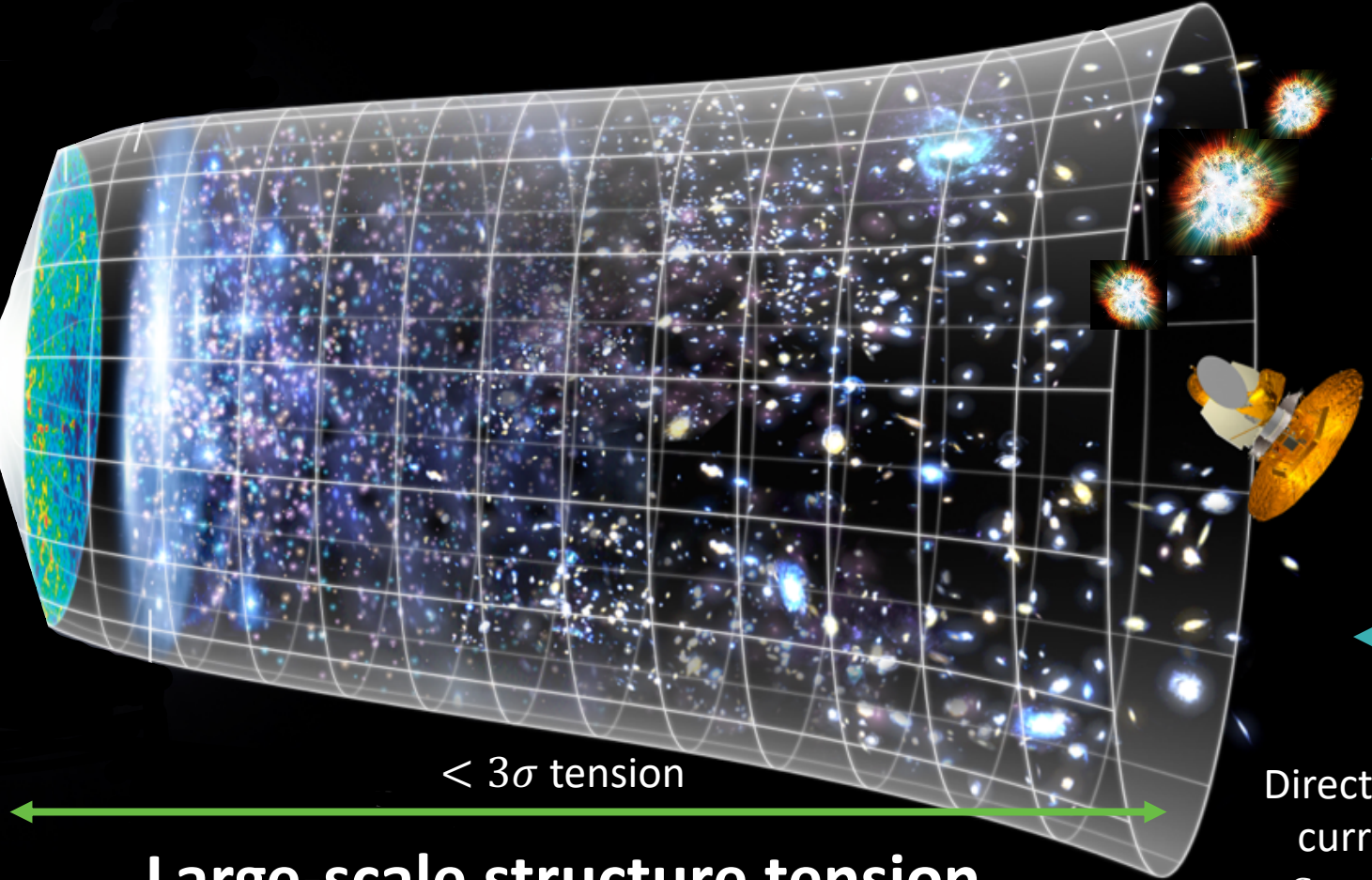
Cosmic microwave background

< 3 $\sigma$  tension

# Large-scale structure tension

Fit  $\Lambda$ CDM to the early universe  
 $S_8 = 0.832 \pm 0.013$

Directly observe the current universe  
 $S_8 = 0.766^{+0.020}_{-0.014}$

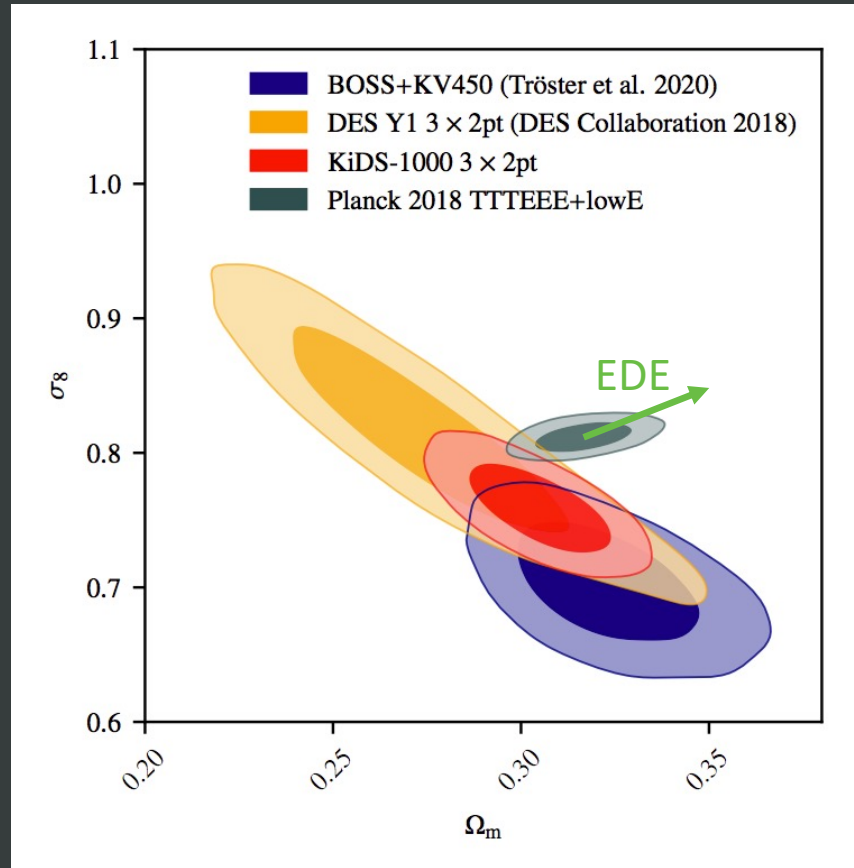


# Challenges for EDE

## Large-scale structure tension and implications

- Gap in our understanding of how matter clusters?
- Insight into dark matter?
- Relate to the small-scale structure problems of  $\Lambda$ CDM?
  - $\Lambda$ CDM has difficulty with galaxy evolution
  - Density distribution of some galaxies – see a core but expect a cusp
  - Missing satellites – we expect more sub-halos than observed

# Challenges for EDE LSS tension



Heymans et al [2007.15632]

## The S8 tension

Large-scale structure  
(LSS) directly observed  
in the late universe

$$S_8 = \sigma_8 \sqrt{\Omega_m / 0.3}$$

<

CMB-inferred value  
using  $\Lambda$ CDM

$$S_8$$

DES Y1 [1708.01530]  
KiDS+VIKING-450 [1812.06076]  
KiDS-1000 [2007.15632]

Consistent

2.3 $\sigma$

3 $\sigma$



# Challenges for EDE

## LSS tension in EDE and $\Lambda$ CDM

Effect of LSS tension on EDE is stronger constraints

EDE with CMB  
 EDE with CMB+LSS  
 $\Lambda$ CDM with CMB+LSS

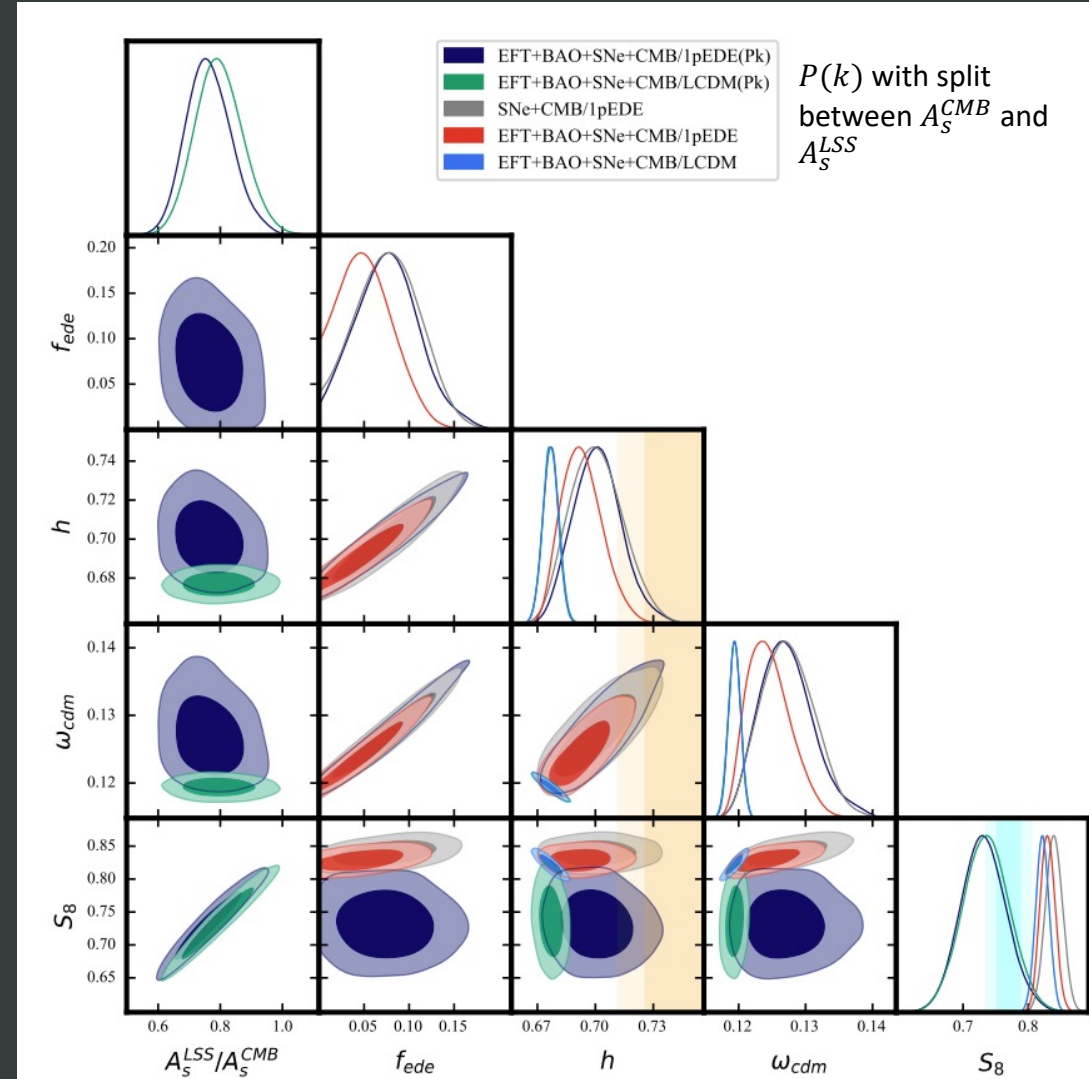
What is the origin of the discrepancy between LSS and CMB?

- Amplitude  $A_s$  of the primordial power spectrum

Exercise: allow LSS and CMB different  $A_s$

$\Lambda$ CDM with CMB+LSS+ $A_s$  split  
 EDE with CMB+LSS+ $A_s$  split

Tight EDE constraints disappear



Smith et al. [2009.10740]

# Towards a new concordance model

Model to replace  $\Lambda$ CDM ?

Model	Tensions
$\Lambda$ CDM	Both $H_0$ and LSS
$\Lambda$ CDM+EDE	Only LSS
New concordance model	Neither

Figure:  
a confused dog

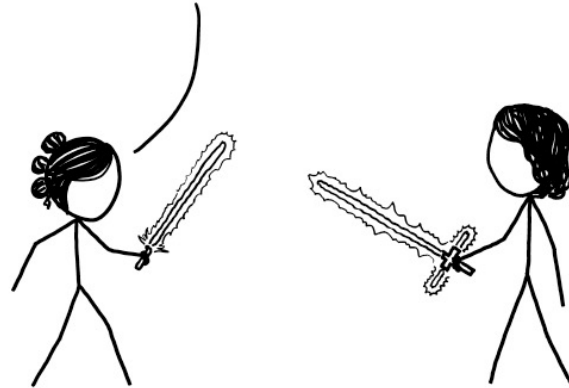


# To EDE and beyond

- Does the Hubble tension indicate new physics? Could a solution lie in the early universe?
- Early dark energy can resolve the Hubble tension
  - Several fundamental models for EDE, with varying success at solving the Hubble tension
  - The goodness of fit to cosmological data is not compromised by this addition
  - CMB data from ACT, SPT and CMB-S4 can test EDE
  - EDE faces challenges with the LSS tension [2003.07355] but this tension arises from within  $\Lambda$ CDM and is not introduced because of EDE [2009.10740]
  - Different avatars of EDE have different effects on the large-scale structure tension?
    - New EDE claims to find no tension with EFT of LSS [2009.00006]
    - EDE coupled to neutrinos might have implications for LSS [1911.11760]
  - EDE can be a stepping-stone as we search for the new concordance model of the Universe
  - Two independent solutions required for  $H_0$  and LSS?
    - $H_0$  depends on background expansion
    - LSS depends on perturbation evolution
  - EDE models can be applied to other eras of cosmic expansion – to explain dark energy or inflation

New LSS, CMB data and further theoretical work might bring insight into the dark sector!

KYLO, WE SHOULDN'T FIGHT! LET'S SET ASIDE OUR DIFFERENCES AND WORK *TOGETHER* TO MEASURE THE LOCAL PROPERTIES OF SPACE, JUST IN CASE SOMEONE IN THE FAR FUTURE IS WATCHING FROM ANOTHER GALAXY AND WANTS OUR HELP TO CONSTRAIN THE EXPANSION RATE!



THE NEW *STAR WARS* TOTALLY PANDERS TO COSMOLOGISTS.

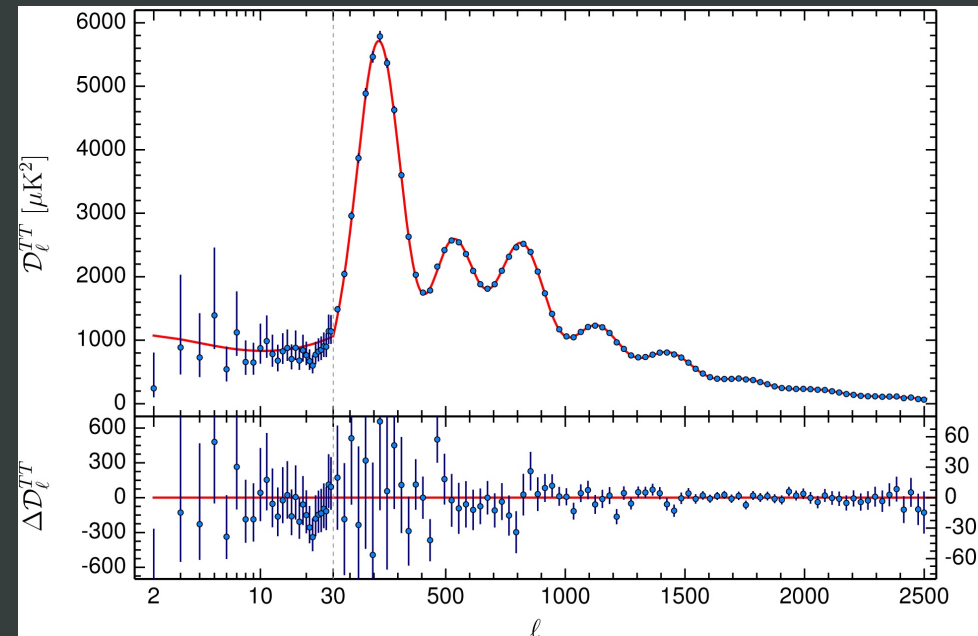
Randall Munroe, xkcd





# $\Lambda$ CDM Parameters

- $H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1}$  - current value of the Hubble parameter
- $\omega_b = \Omega_b h^2$  - the fractional density of baryons in the Universe
- $\omega_c = \Omega_c h^2$  - the fractional density of cold dark matter in the Universe
- $\tau$  - the optical depth due to reionization
- $\ln(10^{10} A_s)$  – amplitude of the primordial power spectrum
- $n_s$  - scalar spectrum power-law index



Source: Ade et al, A&A 2016